



機器人動力與控制

FINAL PROJECT

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OUTLINE

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- 硬體及軟體
- Flow Chart
- 策略及演算法
- 影像辨識
- Q & A
- 實際運作情形

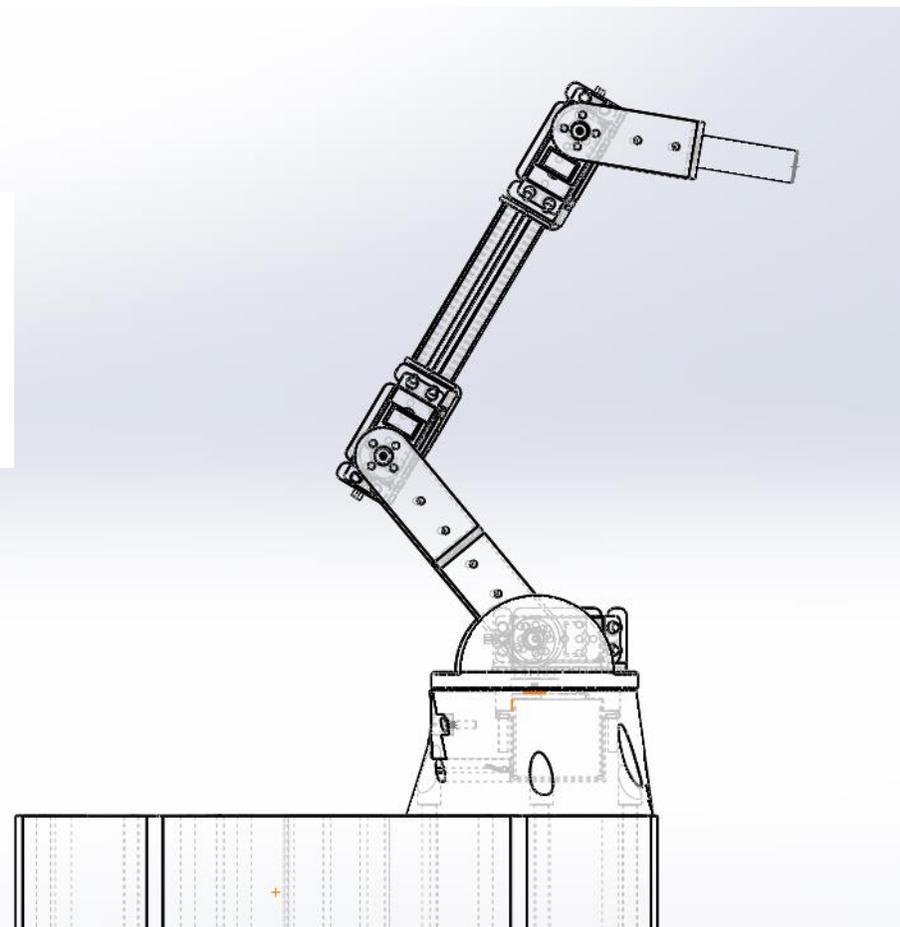
任務及流程

- 讓車體向前移動，同時操控4R手臂使其能在停到目標物前時，讓手臂插進目標物之洞裡
- 車體擺放在某一位置（可看到目標物）→車子移動到目標物旁→手臂移動並依序插進目標物的洞裡（大中小）

硬體—設計和零件組

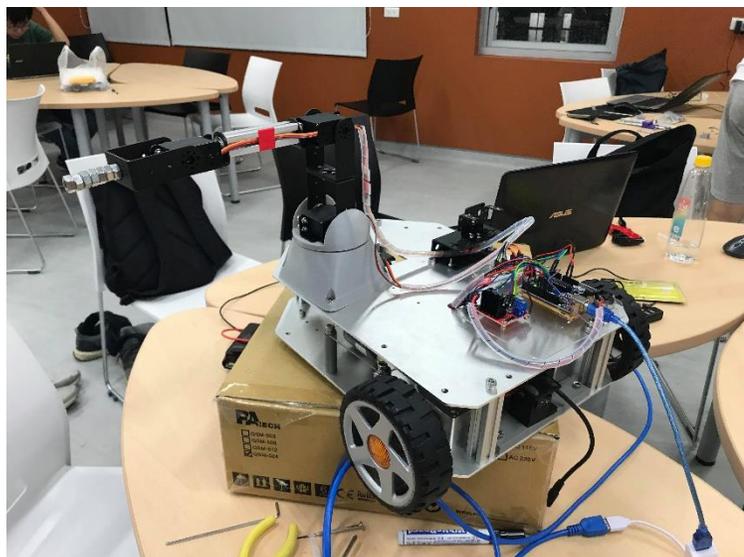
- 車體
- 手臂
- 底座
- 馬達

i	α_{i-1}	a_{i-1}	d_i	θ_i
1	90°	0	23	θ_1
2	0	100.4	0	θ_2
3	0	170	0	θ_3
4	0	95	0	θ_4

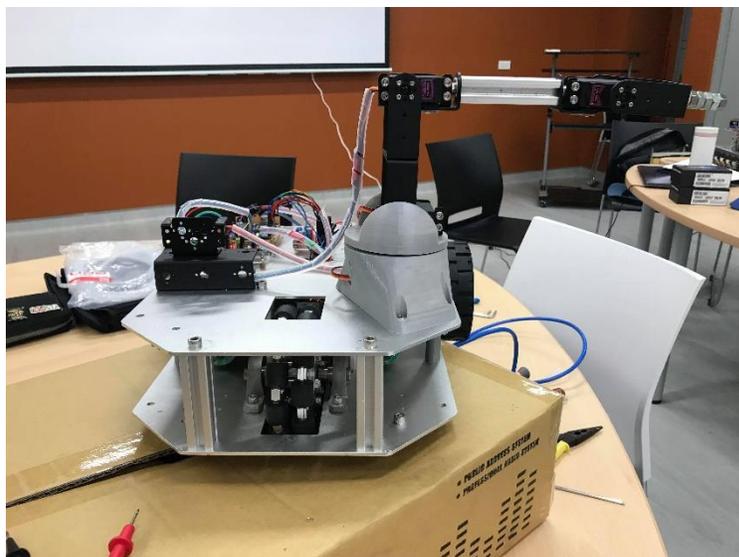


車體

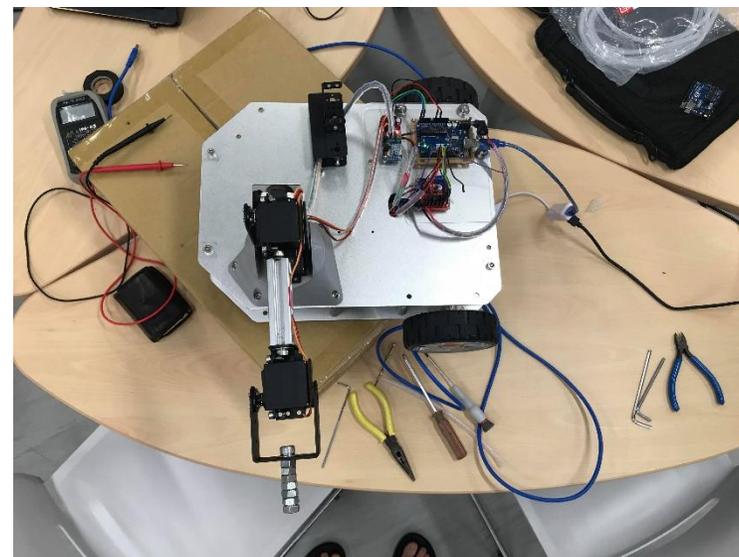
側視圖



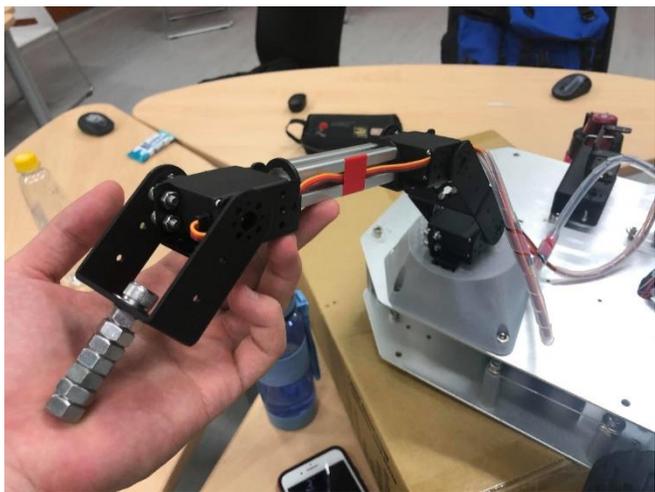
正視圖



上視圖

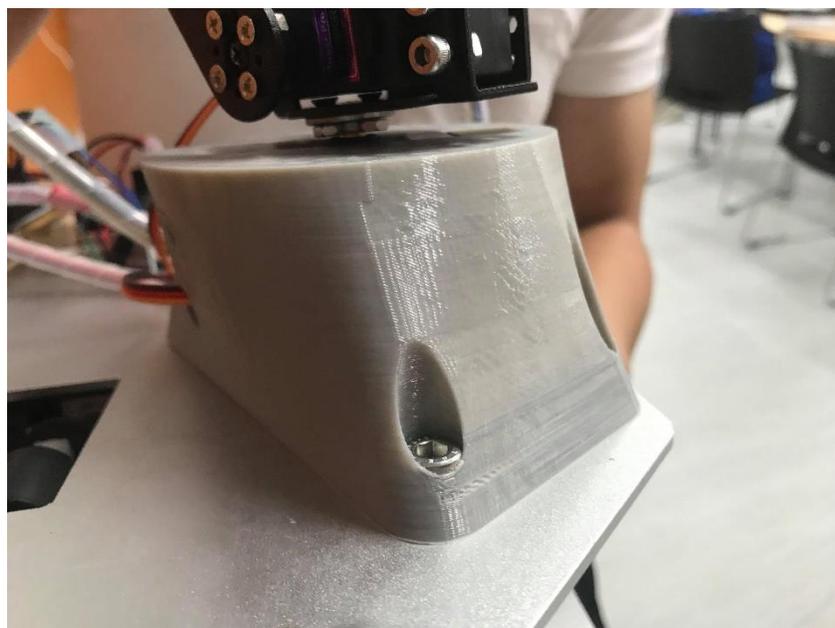


手臂

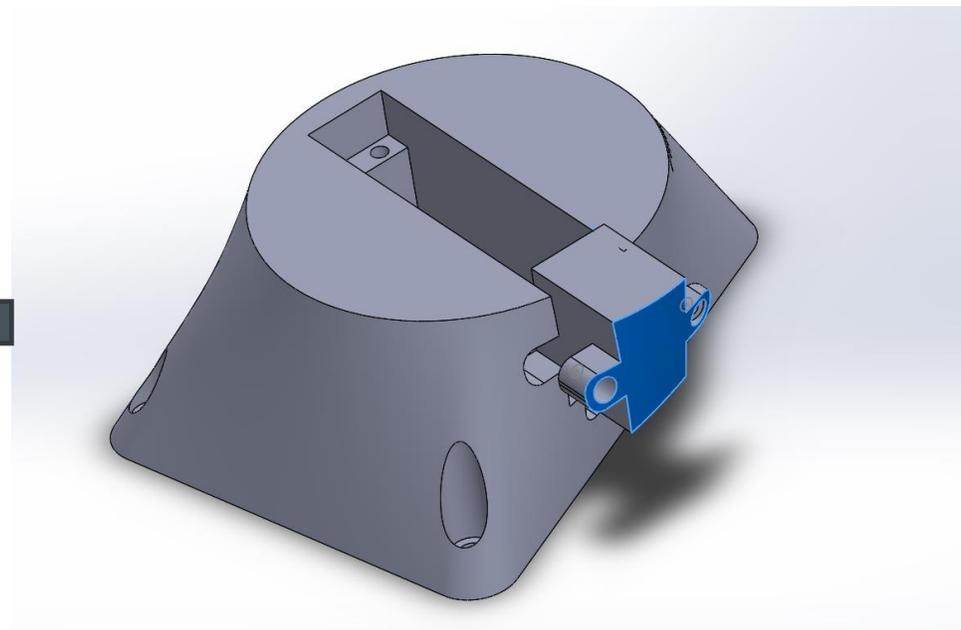


底座

實際圖

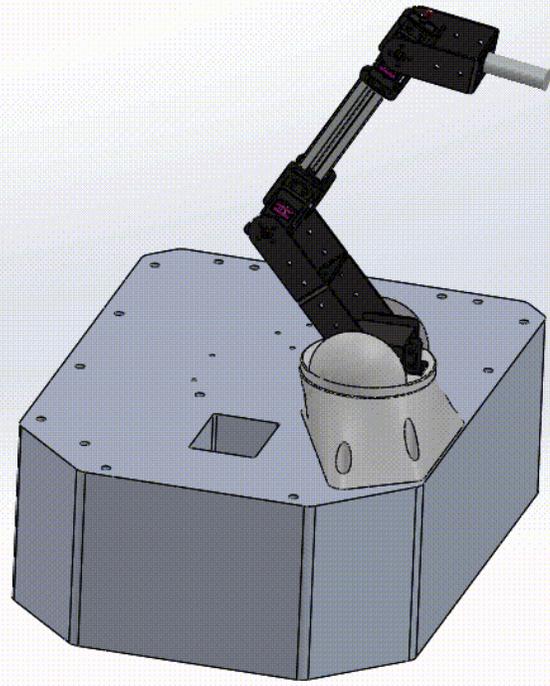


模擬圖



馬達- MG996R、24V DC MOTOR





軟體應用

- Python (上層決策)
- Arduino(底層控制)
- Matlab (模擬)

MATLAB

Inverse Kinematics

Inverse kinematics solution

已知 X, Y, Z 和 $\phi = \theta_2 + \theta_3 + \theta_4$

$$\theta_1 = \tan^{-1}\left(\frac{Y}{X}\right)$$

計算

$$A = X - l_4 \cos\theta_1 \cos\phi$$

$$B = Y - l_4 \sin\theta_1 \cos\phi$$

$$C = Z - l_1 - l_4 \sin\phi$$

得出

$$\theta_3 = \cos^{-1} \frac{A^2 + B^2 + C^2 - l_2^2 - l_3^2}{2 l_2 l_3}$$

再計算

$$a = l_3 \sin\theta_3$$

$$b = l_2 + l_3 \cos\theta_3$$

$$c = Z - l_1 - l_4 \sin\phi$$

$$r = \sqrt{a^2 + b^2}$$

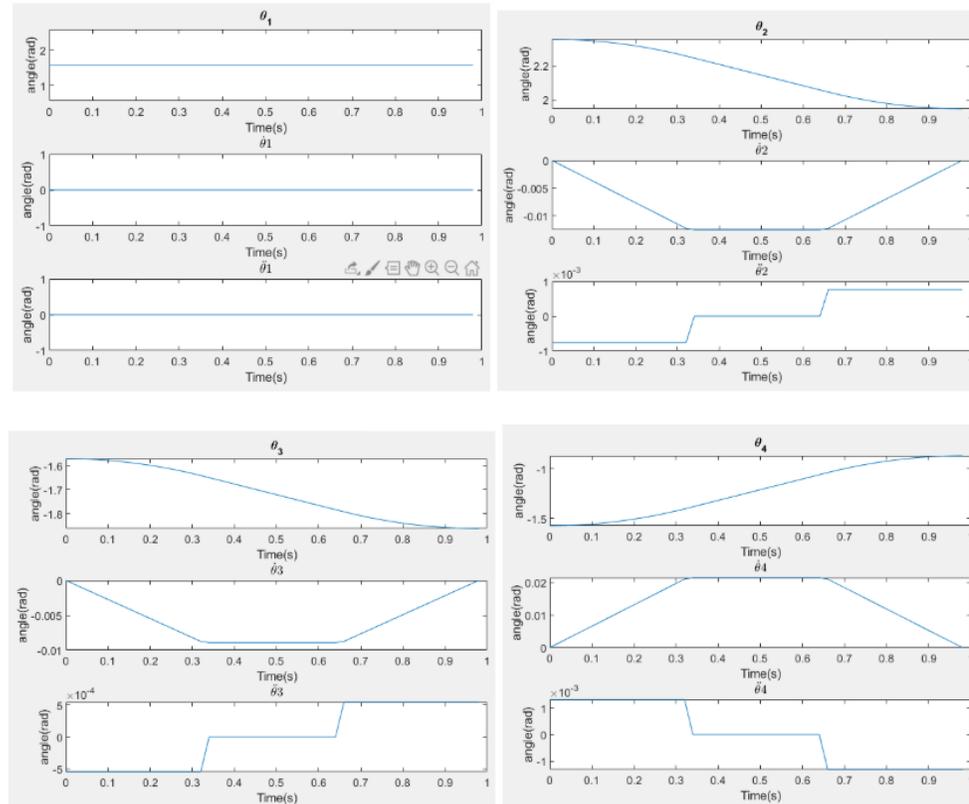
得出

$$\theta_2 = \tan^{-1} \frac{c}{\sqrt{r^2 - c^2}} - \tan^{-1} \frac{a}{b}$$

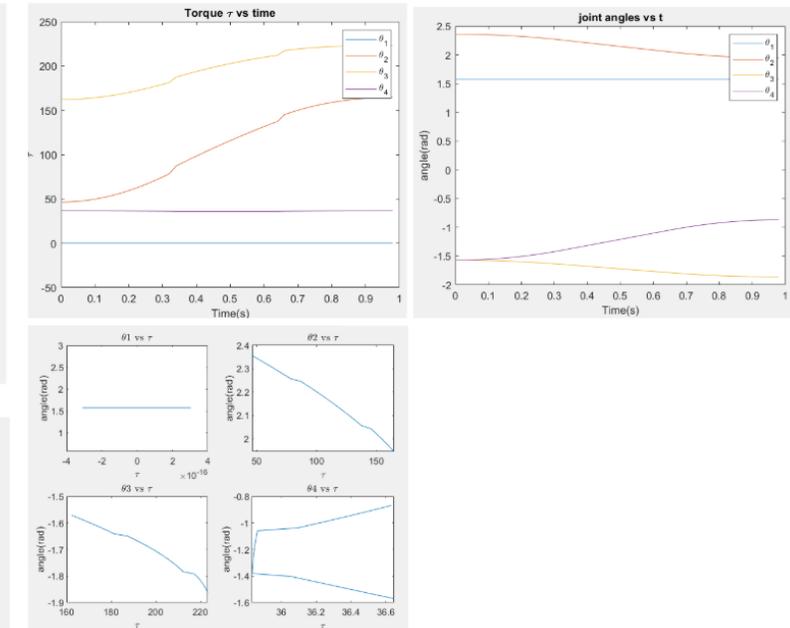
最後可知

$$\theta_4 = \phi - \theta_2 - \theta_3$$

Kinematics simulation

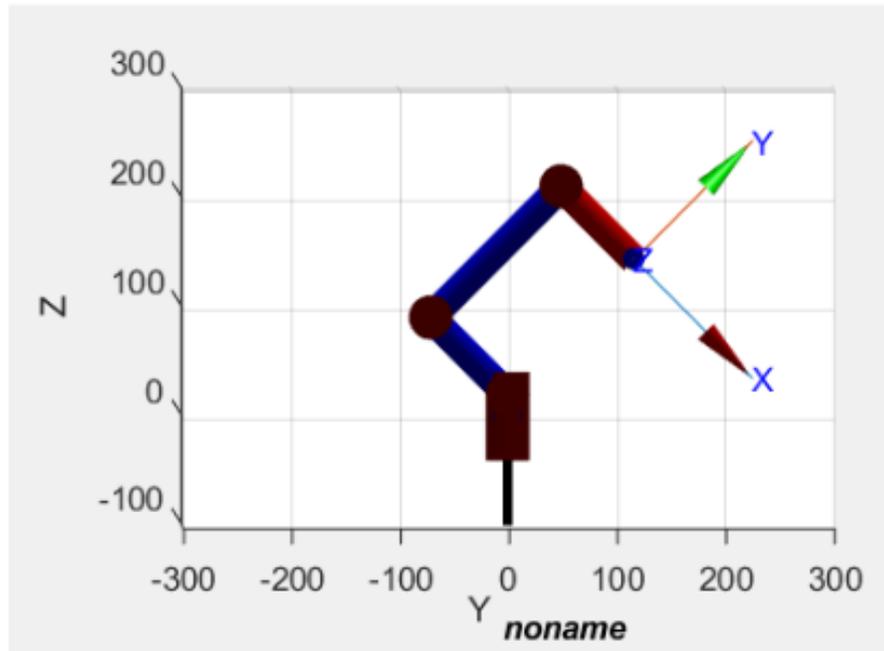


Dynamics Simulation

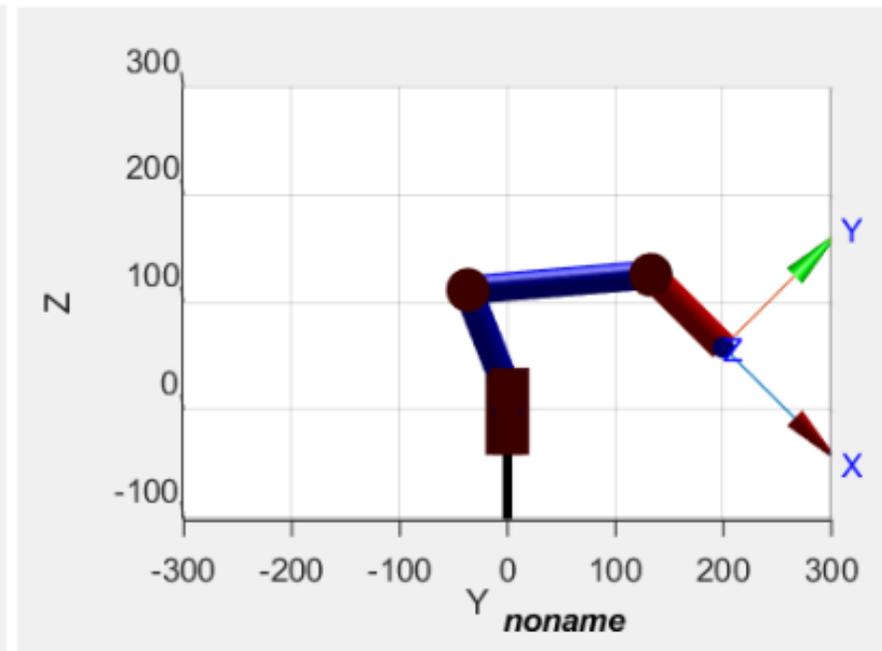


MATLAB

initial position

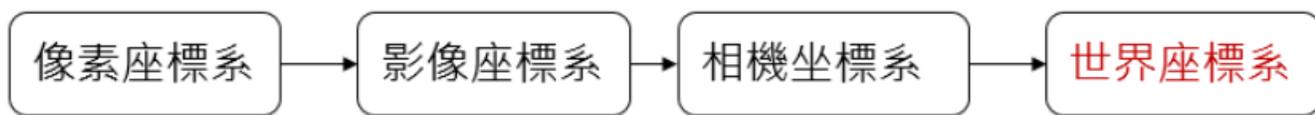


final position



座標系轉換

Coordinate Transform



內部參數(intrinsic parameter):

Realsense d435i

```
camera_cx = 321.798
camera_cy = 239.607
camera_fx = 615.899
camera_fy = 616.468
```

$$\begin{matrix} \text{世界座標} \\ \downarrow \\ \begin{bmatrix} X_w \\ Y_w \\ Z_w \\ 1 \end{bmatrix} \end{matrix} = \begin{matrix} \begin{bmatrix} {}^W_C R & {}^W P_{CORG} \\ 0 & 1 \end{bmatrix} \\ \text{外部參數} \end{matrix} \begin{matrix} \begin{bmatrix} \frac{Z_c}{camera_fx} & 0 & \frac{-Z_c camera_cx}{camera_fx} \\ 0 & \frac{Z_c}{camera_fy} & \frac{-Z_c camera_cy}{camera_fy} \\ 0 & 0 & Z_c \\ 0 & 0 & 1 \end{bmatrix} \\ \text{內部參數} \end{matrix} \begin{matrix} \text{像素座標} \\ \downarrow \\ \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} \end{matrix}$$

外部參數

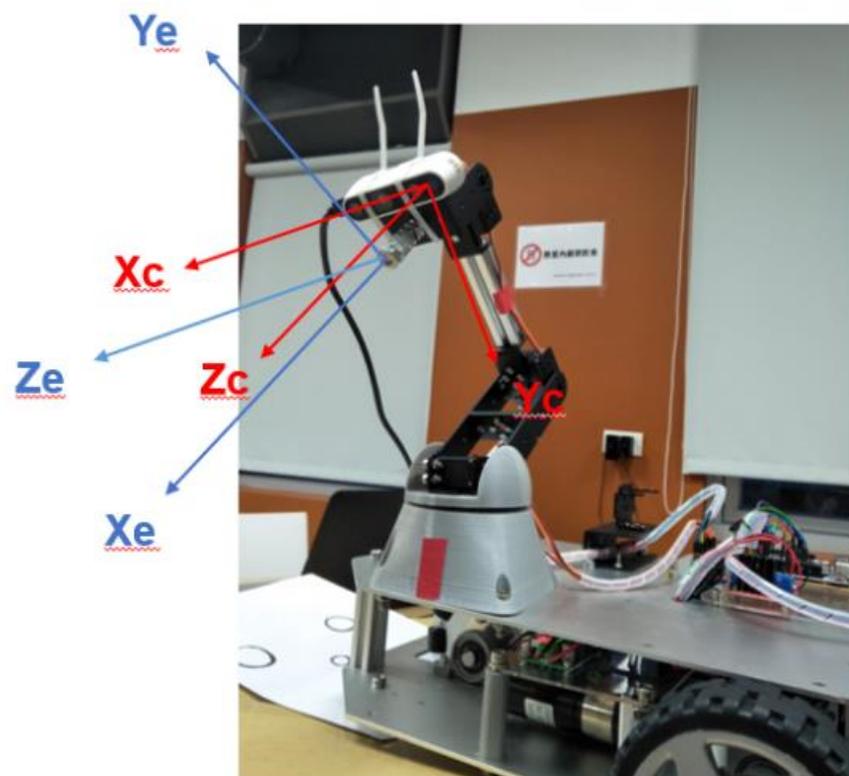
內部參數

外部參數(extrinsic parameter):

外部參數=手臂順向Transform matrix * Rotation matrix

Rotation matrix:使相機座標系與手臂end_effeter 的方向一致

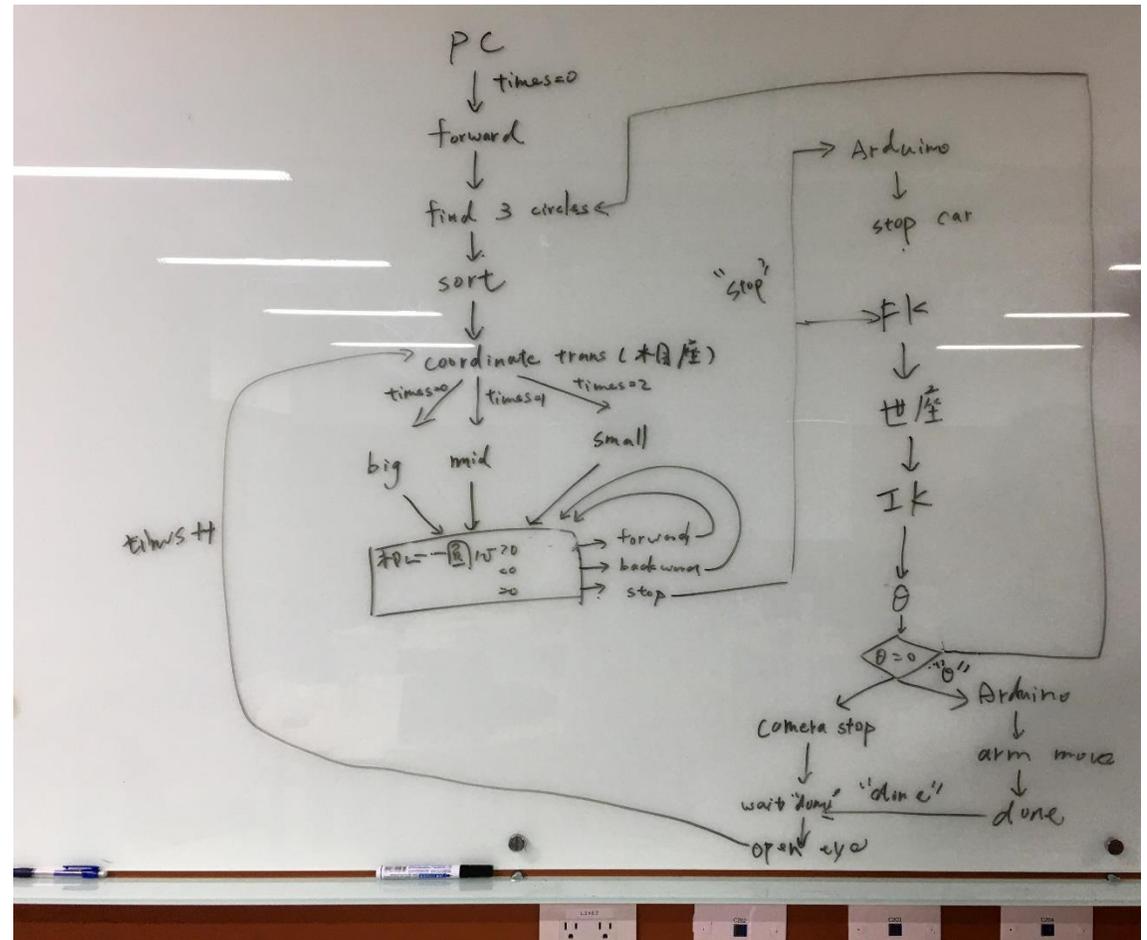
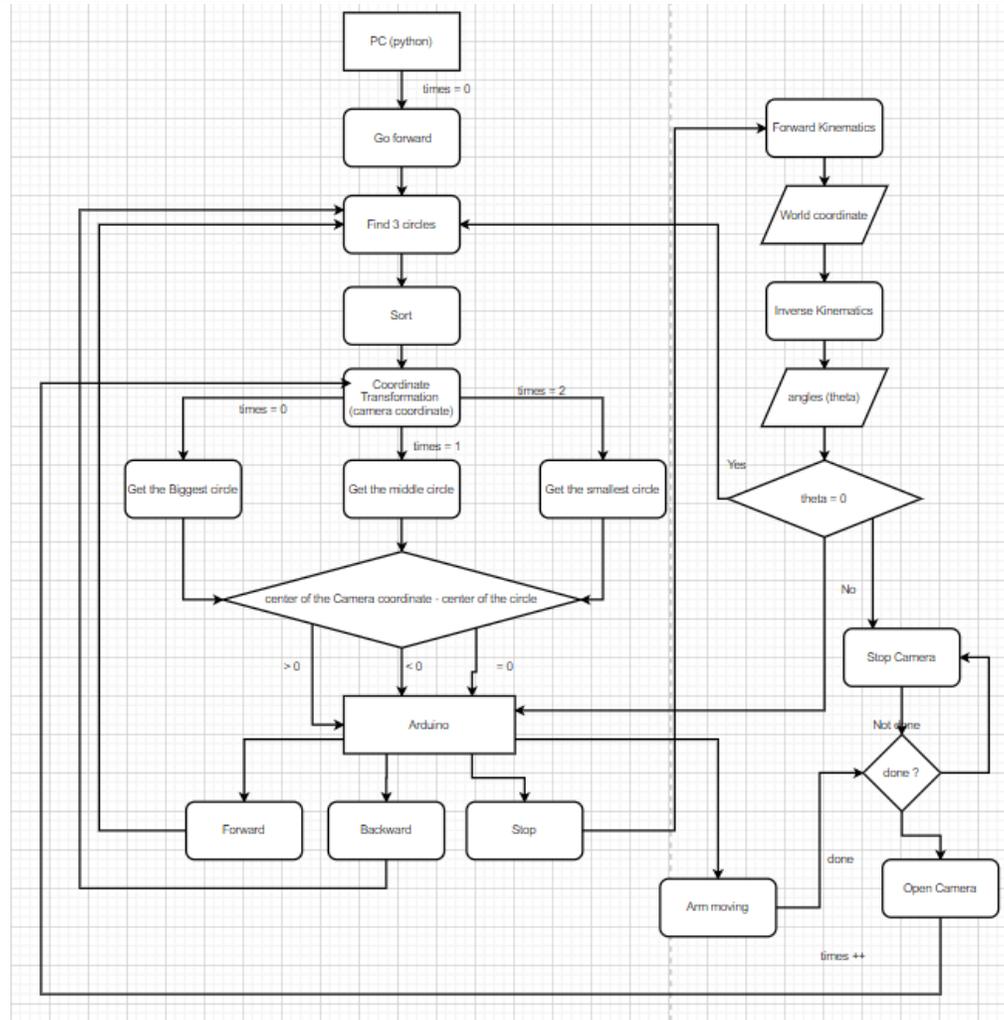
座標系轉換



(X_c, Y_c, Z_c) :相機坐標系

(X_e, Y_e, Z_e) :end_effector坐標系

FLOW CHART



車體控制

pseudo code:

```
目標物在車體右邊
k = 0.30      #gain
if 找到三個圓:
    將圓從大排到小
    if (相機中心-圓中心) < 30mm:
        velocity = 0
    else :
        velocity = (相機中心-圓中心) * k

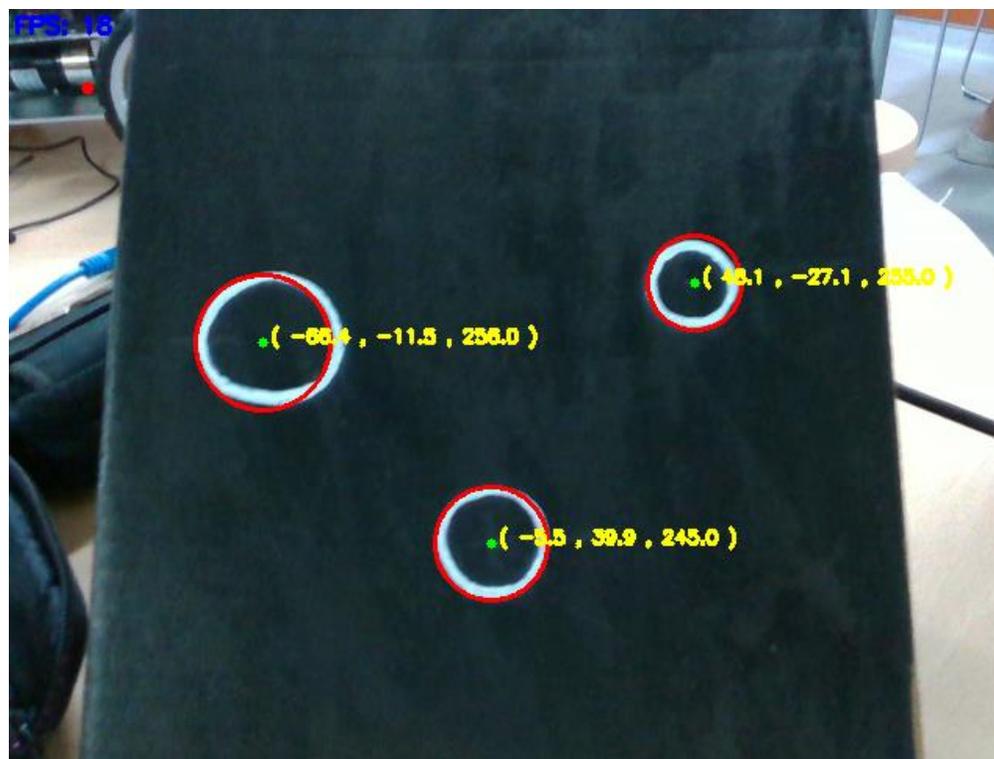
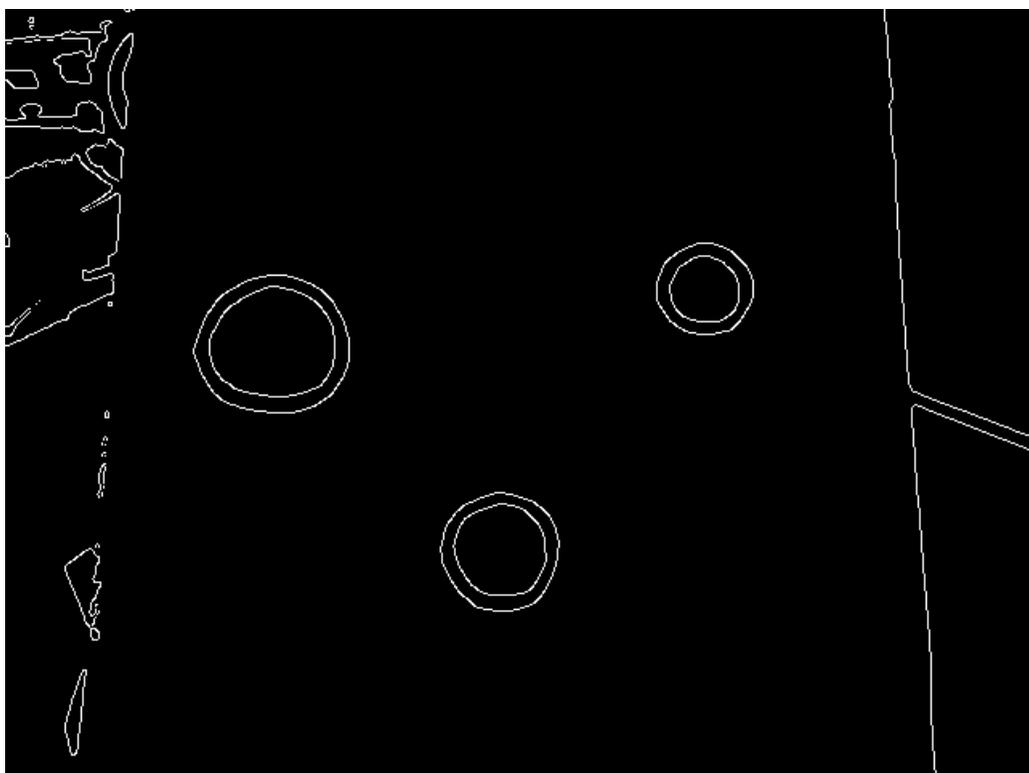
    if velocity > 0:
        go backward
    else:
        go forward
else:
    跑很快
```

```
k = 0.5
if np.size(coordinate,0) == 3:
    coordinate = rad_sort(coordinate)
    if -coordinate[0][0] < 10:
        vel = 0
    else :
        vel = -coordinate[0][0] * k

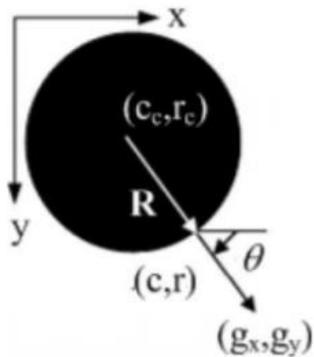
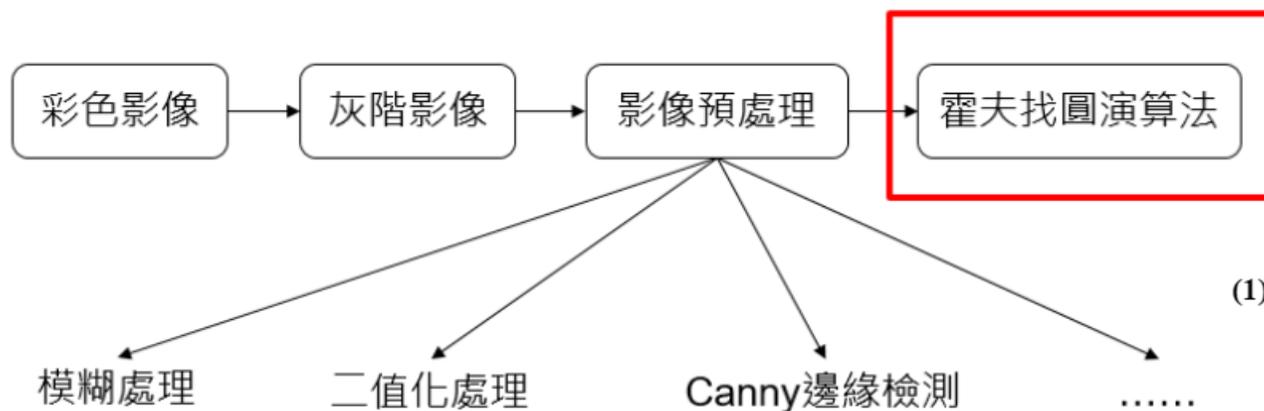
    if vel < 0:
        vel = -vel
        velocity = str(vel) + "," + "1\n"
    else:
        velocity = str(vel) + "," + "0\n"

    ser.write(velocity.encode())
else:
    ser.write(("50,0\n").encode())
```

影像辨識



影像辨識演算法



$$(c - c_c)^2 + (r - r_c)^2 = R^2$$

$$c_c = c - R \cos \theta$$

$$r_c = r - R \sin \theta$$

$$\cos \theta = \frac{g_x}{\sqrt{g_x^2 + g_y^2}}$$

$$\sin \theta = \frac{g_y}{\sqrt{g_x^2 + g_y^2}}$$

g_x : gradient in x axis

g_y : gradient in y axis

Implementation

(1) 初始化一個三維累加器 $accu = (X_C, Y_C, R)$ ，分別代表圓心X座標，圓心Y座標及圓半徑R

(2) 利用 **sobel filter** 取出圓形的 g_x, g_y

(3) 給定圓半徑R的最大 R_{max} 及最小值 R_{min}

(4) 利用下式:

$$X_C = x - R \cos \theta$$

$$Y_C = y - R \sin \theta$$

對每一個R及圓心pixel座標(x,y)求出圓心(X_C, Y_C)

(5) 將累加器 $accu(X_C, Y_C, R) + 1$

(6) 得到 $accu$ 最大的值及求得圓的圓心及半徑

Q&A



實際運作情形

- 請見7/3下午兩點半



THANKS FOR LISTENING